

## **ADVANCED GRAPH THEORY**

Course No: <b>MM 17304DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

#### **Colorings**

Vertex coloring, chromatic number  $\chi(G)$ , bounds for  $\chi(G)$ , Brook's theorem, edge coloring, Vizing's theorem, map coloring, six color theorem, five color theorem, every graph is four colourable iff every cubic bridgeless plane map is 4-colorable, every planar graph is 4-colorable iff  $\chi'(G) \leq 3$ , Heawood map-coloring theorem, uniquely colorable graphs

### **UNIT -II**

#### **Matchings**

Matchings and 1-factors, Berge's theorem, Hall's theorem, 1-factor theorem of Tutte, antifactor sets, f-factor theorem, f-factor theorem implies 1-factor theorem, Erdos- Gallai theorem follows from f-factor theorem, degree factors, k-factor theorem, factorization of  $K_n$ .

### **UNIT -III**

#### **Edge graphs and eccentricity sequences**

Edge graphs, Whitney's theorem on edge graphs, Beineke's theorem, edge graphs of trees, edge graphs and traversability, total graphs, eccentricity sequences and sets, Lesniak theorem for trees, construction of trees, neighbourhoods, Lesniak theorem graphs.

### **UNIT -IV**

#### **Groups in graphs and graph spectra**

Automorphism groups of graphs, graph with a given group, Frucht's theorem, Cayley digraph, spectrum of a graph, spectrum of some graphs-regular graph, compliment of a graph, edge graph, complete graph, complete bipartite, cycle and path, Laplacian spectrum, energy of a graph, Laplacian energy.

**Recommended Books:**

1. R. Balakrishnan, K. Ranganathan, A Text Book of Graph Theory, Springer-Verlag, New York
2. B. Bollobas, Extremal Graph Theory, Academic Press.
3. F. Harary, Graph Theory, Addison-Wesley.
4. Narsingh Deo, Graph Theory with Applications to Engineering and Computer Science, Prentice Hall
5. S. Pirzada, An Introduction to Graph Theory, Universities Press, Orient Blackswan, 2012
6. W. T. Tutte, Graph Theory, Cambridge University Press.
7. D. B. West, Introduction to Graph Theory, Prentice Hall

## **ABSTRACT MEASURE THEORY**

Course No. **MM 17305DCE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Semiring , algebra and  $\sigma$  - algebra of sets, Borel sets, measures on semirings, outer measure associated with a set function and basic properties, measurable sets associated with an outer measure as a  $\sigma$  - algebra , outer measure induced by a measure, non-measurable sets.

### **UNIT -II**

Improper Riemann integral as a Lebesgue integral, calculation of some improper Riemann integrable functions, Riemann Lebesgue lemma, product measures and integrated integrals, examples of non-integrable functions whose iterated integrals exist, Fubini theorem.

#### **Recommended Books:**

1. C.D.Aliprantis and O.Burkinshaw, Principles of Real Analysis.
2. R.Goldberg, Methods of Real Analysis.
3. T.M.Apostol, Mathematical Analysis.

#### **References:**

1. L.Royden, Real Analysis (PHI)
2. S.B.Chae, Lebesgue Integration(Springer Verlag).
3. W.Rudin, Principles of Mathematical Analysis (McGraw Hill).
4. G.De.Barra , Measure Theory and Integration ( Narosa).
5. I.K.Rana, An Introduction to Measure and Integration, Narosa Publications.

## **MATHEMATICAL BIOLOGY**

Course No: <b>MM 17306DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Diffusion in biology: Fick's law of diffusion, Fick's perfusion law, membrane transport, diffusion through a slab, convective transport, transcapillary exchange, heat transport in biological tissues, oxygen transport through red cells, gas exchange in lungs, the ideal gas law and solubility of gases, the equation of gas transport in one Alveolus.

### **UNIT -II**

Biofluid mechanics: introduction, various types of fluid flows, viscosity, basic equation of fluid, mechanics, continuity equation, equation of motion, the circulatory system, systemic and pulmonary circulation, the circulation in heart, blood composition, arteries and arterioles, models in blood flow, Poiseuille's flow and its applications, the pulse wave.

### **UNIT -III**

Tracers in physiological systems: compartment systems, the one compartment system, discrete and continuous transfers, ecomatrix, the continuous infusion, the two compartment system, bath-tub models, three-compartment system, the leaky compartment and the closed systems, elementary pharmacokinetics, parameter estimation in two compartment models, basic introduction to n-compartment systems.

### **UNIT -IV**

Biochemical reactions and population genetics: the law of mass action, enzyme kinetics, Michael's- Menten theory, competitive inhibition, Allosteric inhibition, enzyme-substrate-inhibitor system, cooperative properties of enzymes, the cooperative dimer, haemoglobin. haploid and diploid genetics, spread of favourite allele, mutation-selection balance, heterosis, frequency dependent selection.



**Books Recommended**

1. J.D. Murray, Mathematical Biology, CRC Press
2. S.I. Rubinow, Introduction to Mathematical Biology, John Wiley and Sons.
3. Guyton and Hall, Medical Physiology.
4. S.C. Hoppersteadt and C.S. Peskin, Mathematics in Medicine and Life Sciences, Springer-Verlag
5. J.R. Chesnov, Lecture notes in Mathematical Biology, Hong Kong Press
6. J. N. Kapur, Mathematical methods in Biology and Medicine, New Age Publishers
7. D. Ingram and R.F. Bloch, Mathematical methods in Medicine, John Wiley and Sons.

## **WAVELET THEORY**

Course No: <b>MM 17307DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

#### **Time Frequency Analysis and Wavelet Transforms**

Gabor transforms, basic properties of Gabor transforms, continuous and discrete wavelet transforms with examples, basic properties of wavelet transforms, examples of Haar wavelet, Mexican hat wavelet and their Fourier transforms, dyadic orthonormal wavelet bases for  $L^2(\mathbb{R})$ .

### **UNIT -II**

#### **Multiresolution Analysis and Construction of Wavelets**

Definition and examples of multiresolution analysis (MRA), properties of scaling functions and orthonormal wavelet bases, construction of orthonormal wavelets with special reference to Haar wavelet, Franklin wavelet and Battle-Lemarie wavelet, Spline wavelets, construction of compactly supported wavelets, Daubechie's wavelets and algorithms.

### **UNIT -III**

#### **Other Wavelet Constructions and Characterizations**

Introduction to basic equations, some applications of basic equations, characterization of MRA wavelets and scaling functions, construction of biorthogonal wavelets, wavelet packets, definition and examples of wavelets in higher dimensions.

## **UNIT -IV**

### **Further Extensions of Multiresolution Analysis**

Periodic multiresolution analysis and the construction of periodic wavelets, multiresolution analysis associated with integer dilation factor (M-band wavelets), harmonic wavelets, properties of harmonic scaling functions.

#### **Recommended Books:**

1. L. Debnath, Wavelet Transforms and their Applications, Birkhauser, 2002.
2. I. Daubechies, Ten Lectures on Wavelets, CBS-NSF Regional Conferences in Applied Mathematics, 61, SIAM, Philadelphia, PA, 1992.
3. K. Ahmad and F. A. Shah, Introduction to Wavelets with Applications, Real World Education Publishers, New Delhi, 2013.

#### **References:**

1. C. K. Chui, An Introduction to Wavelets, Academic Press, New York, 1992.
2. M. Pinsky, Introduction to Fourier Analysis and Wavelets, Brooks/Cole, 2002.
3. E. Hernandez and G. Weiss, A First Course on Wavelets, CRC Press, New York (1996).

## **LINEAR ALGEBRA**

Course No: **MM 17308DCE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Linear transformation, algebra of linear transformations, linear operators, invertible linear transformations, matrix representation of a Linear transformation, linear functionals, dual spaces, dual basis, annihilators, eigen values and eigen-vectors of linear transformation, diagonalization, similarity of linear transformation.

### **UNIT -II**

Canonical forms: triangular form, invariance, invariant direct sum decomposition, primary decomposition, nilpotent operators, Jordan canonical form, cyclic subspaces, rational canonical form, quotient spaces, bilinear forms, alternating bilinear forms, symmetric bilinear forms, quadratic forms.

### **Books Recommended:**

1. Robert A. Beezer, A first course in linear algebra.
2. John B. Fraleigh and Raymond, Linear Algebra.
3. A. K. Sharma, Linear Algebra.
4. Vivek Sahai and Vikas Bist, Linear Algebra.

## **ANALYTIC THEORY OF POLYNOMIALS**

Course No: <b>MM 17404DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Introduction, the fundamental theorem of algebra(revisited), symmetric polynomials, the continuity theorem, orthogonal polynomials, general properties, the classical orthogonal polynomials, tools from matrix analysis.

### **UNIT -II**

Critical points in terms of zeros, fundamental results and critical points, convex hulls and Gauss-Lucas theorem, some applications of Gauss-Lucas theorem, extensions of Gauss-Lucas theorem, average distance from a line or a point, real polynomials and Jensen's theorem, extensions of Jensen's theorem.

### **UNIT -III**

Derivative estimates on the unit interval, inequalities of S. Bernstein and A. Markov, extensions of higher order derivatives, two other extensions, dependence of the bounds on the zeros, some special classes,  $L^p$  analogous of Markov's inequality.

### **UNIT -IV**

Coefficient estimates, polynomials on the unit circles, coefficients of real trigonometric polynomials, polynomials on the unit interval.

#### **Recommended Books:**

1. Q. I. Rahman and G.Schmeisser, Analytic Theory of Polynomials.
2. Morris Marden, Geometry of Polynomials.
3. G. V. Milovanovic, D.S.Mitrinovic and Th. M. Rassias, Topics in Polynomials, Extremal Properties, Problems, Inequalities, Zeroes.
4. G. Polya and G. Szego, Problems and Theorems in Analysis ( Springer Verlag New York Heidelberg Berlin).

## **MATHEMATICAL STATISTICS**

Course No: <b>MM 17405DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Some Special Distributions, Bernoulli, Binomial, trinomial, multinomial, negative binomial, Poisson, gamma, chi-square, beta, Cauchy, exponential, geometric, normal and bivariate normal distributions.

### **UNIT -II**

Distribution of functions of random variables, distribution function method, change of variables method, moment generating function method, t and F distributions, Dirichelet distribution, distribution of order statistics, distribution of  $X$  and  $\frac{nS^2}{\sigma^2}$ , limiting distributions, different modes of convergence, central limit

### **UNIT -III**

Interval estimation, confidence interval for mean, confidence interval for variance, confidence interval for difference of means and confidence interval for the ratio of variances, point estimation, sufficient statistics, Fisher-Neyman criterion, factorization theorem, Rao- Blackwell theorem, best statistic (MvUE), Complete Sufficient Statistic, exponential class of pdfs.

### **UNIT -IV**

Rao-Crammer inequality, efficient and consistent estimators, maximum likelihood estimators (MLE's), testing of hypotheses, definitions and examples, best or most powerful (MP) tests, Neyman Pearson theorem, uniformly most powerful (UMP) tests, likelihood ratio test, chi-square test.

### **Recommended Books**

1. Hogg and Craig, An Introduction to Mathematical Statistics.
2. Mood and Grayball, An Introduction to Mathematical Statistics.

### **References**

1. C. R. Rao, Linear Statistical Inference and its Applications.
2. V. K. Rohatgi, An Introduction to Probability and Statistics.

## **FUNCTIONAL ANALYSIS-II**

Course No: <b>MM 17406DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Relationship between analytic and geometric forms of Hahn-Banach theorem, applications of Hahn-Banach theorem, Banach limits, Markov-Kakutani theorem for a commuting family of maps, complemented subspaces of Banach spaces, complementability of dual of a Banach space in its bidual, uncomplementability of  $c_0$  in  $l_\infty$ .

### **UNIT -II**

Dual of subspaces, quotient spaces of a normed linear space, weak and weak\* topologies on a Banach space, Goldstine's theorem, Banach Alaoglu theorem and its simple consequences, Banach's closed range theorem, injective and surjective bounded linear mappings between Banach spaces.

### **UNIT -III**

$l_\infty$  and  $C[0,1]$  as universal separable Banach spaces,  $l_1$  as quotient universal separable Banach spaces, Reflexivity of Banach spaces and weak compactness, Completeness of  $L_p[a,b]$ , extreme points, Krein-Milman theorem and its simple consequences.

### **UNIT -IV**

Dual of  $l_\infty$ ,  $C(X)$  and  $L_p$  spaces. Mazur-Ulam theorem on isometries between real normed spaces, Muntz theorem in  $C[a,b]$ .

### **Recommended Books:**

1. J. B. Conway, A First Course in Functional Analysis (Springer Verlag).
2. R. E. Megginson, An Introduction to Banach Space theory (Springer Verlag, GTM, Vol. 183)
3. Lawrence Baggett, Functional Analysis, A Primer (Chapman and Hall, 1991).

### **References:**

1. B. Bollobas, Linear Analysis (Camb. Univ.Pres).
2. B. Beauzamy, Introduction to Banach Spaces and their geometry ( North Holland ).
3. Walter Rudin, Functional Analysis (Tata McGrawHill).



## **NON-LINEAR ANALYSIS**

Course No: <b>MM 17407DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Convex Sets, best approximation properties, topological properties, separation, nonexpansive operators, projectors onto convex sets, fixed points of nonexpansive operators, averaged nonexpansive operators, Fejer monotone sequences, convex cones, generalized interiors, polar and dual cones, tangent and normal cones, convex functions, variants, between linearity and convexity, uniform and strong convexity, quasiconvexity

### **UNIT -II**

Gateaux Derivative, Frechet Derivative, lower semicontinuous convex functions, subdifferential of convex functions, directional derivatives, characterization of convexity and strict convexity, directional derivatives and subgradients, Gateaux and Frechet differentiability, differentiability and continuity

### **UNIT -III**

Monotone operators, strong notions of monotonicity such as para, cyclic, strict, uniform and strong monotonicity, maximal monotone operator and their properties, bivariate functions and maximal monotonicity, Debrunner-Flor theorem, Minty theorem, Rockfeller's cyclic monotonicity theorem, monotone operators on  $R$ .

### **UNIT -III**

Reisz-Representation theorem, projection mappings and their properties, characterization of projection onto convex sets and their geometrical interpretation,

Billinear forms and its applications, Lax-Milgram lemma, minimization of functionals, variational inequalities, relationship between abstract

minimization problems and variational inequalities, Lions Stampacchia theorem for existence of solution of variational inequality.

### **Recommended Books:**

1. H. H. Bauschke and P. L. Combettes, Convex Analysis and Monotone Operator Theory in Hilbert Spaces, Springer New York, 2011.
2. D. Kinderlehrer and G. Stampacchia, An Introduction to Variational Inequalities and Their Applications, Academic Press, New York, 1980.
3. A. H. Siddiqi, K. Ahmed and Manchanda, P. Introduction to Functional Analysis with Applications, Anamaya Publishers, New Delhi-2006.

### **References:**

1. I. Ekeland and R. Temam, Convex Analysis and Variational Problems, W.Takahashi, Nonlinear Functional Analysis, North-Holland Publishing Company-Ammsterdam, 1976.
2. M. C. Joshi and R. K. Bose, Nonlinear Functional Analysis and its Applications, Willey Eastern Limited, 1985.

## **ADVANCED TOPICS IN TOPOLOGY AND MODERN ANALYSIS**

Course No: <b>MM 17408DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Uniform spaces, definition and examples, uniform topology, metrizability complete regularity of uniform spaces, pre-compactness and compactness in uniform spaces, uniform continuity.

### **UNIT II**

Uniform continuity, uniform continuous maps on compact spaces Cauchy convergence and completeness in uniform spaces, initial uniformity, simple applications to function spaces, Arzela- Ascoli theorem.

### **UNIT -III**

Abstract harmonic analysis, definition of a topological group and its basic properties. subgroups and quotient groups, product groups and projective limits, properties of topological groups involving connectedness, invariant metrics and Kakutani theorem, structure theory for compact and locally compact, Abelian groups.

### **UNIT -IV**

Some special theory for compact and locally compact Abelian groups, Haar integral and Haar measure, invariant means defined for all bounded functions, convolution of functions and measures, elements of representation theory, unitary representations of locally compact groups.

#### **Recommended Books:**

1. I. M. James, Uniform Spaces, Springer Verlag.
2. K. D. Joshi, Introduction to General Topology.
3. S. K. Berberian, Lectures on Operator Theory and Functional Analysis, Springer Verlag.
4. G. B. Folland, Real Analysis, John Wiley.

#### **References:**

1. G. Murdeshwar, General Topology.
2. E. Hewitt & K.A Ross, Abstract Harmonic Analysis-I, Springer Verlag.

## **PROJECT**

Course No: <b>MM 17409DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

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The student opting for project will have to work on the research problem in any one of the following areas:

- i. **Complex Analysis**
- ii. **Functional Analysis**
- iii. **Graph Theory and Algebra**
- iv. **Mathematical Biology**

The student will be put under the guidance of faculty member of the respective areas. At the end the student will have to submit dissertation. The dissertation will carry 80 marks following which there will be a viva-voce examination carrying 20 marks.

## **THEORY OF MATRICES**

Course No: **MM18105DCE**

**Examination:**

(a). Assessment

(b). Theory

Total Credits: **04**

**Total Marks: 100**

Max. Marks: 20

Max. Marks: 80

### **UNIT-I**

Eigen values and eigen vectors of a matrix and their determination, similarity of matrices, two similar matrices have the same eigen values, algebraic and geometric multiplicity, necessary and sufficient condition for a square matrix of order  $n$  to be similar to a diagonal matrix, orthogonal reduction of real matrices.

### **UNIT-II**

Orthogonality of the eigen vectors of a Hermitian matrix, the necessary and sufficient condition for a square matrix of order  $n$  to be similar to a diagonal matrix. If  $A$  is a real symmetric matrix then there exists an orthogonal matrix  $P$  such that  $P^{-1}AP = P^TAP$  is a diagonal matrix whose diagonal elements are the eigen values of  $A$ , semi-diagonal or triangular form, Schur's theorem, normal matrices, necessary and sufficient condition for a square matrix to be unitarily similar to a diagonal matrix.

### **UNIT-III**

Quadratic forms: the Kroneckers and Lagranges reduction, reduction by orthogonal transformation of real quadratic forms, necessary and sufficient condition for a quadratic form to be positive definite, rank, index and signature of a quadratic form. If  $A=[a_{ij}]$  is a positive definite matrix of order  $n$ , then  $|A| \leq a_{11} a_{22} \dots a_{nn}$ .

### **UNIT IV**

Gram matrices: the Gram matrix  $BB^T$  is always positive definite or positive semi-definite, Hadamard's inequality, If  $B=[b_{ij}]$  is an arbitrary non-singular real square matrix of order  $n$ , then  $|B| \leq \prod_{i=1}^n [\sum_{k=1}^n b_{ik}^2]$ , functions of symmetric matrices, positive definite square root of a positive definite matrix, the infinite  $n$ -fold integral

$$I_n = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \cdots \int_{-\infty}^{\infty} e^{-X'AX} dX,$$

where  $dX = dx_1 dx_2 \cdots dx_n$ . If A is a positive definite matrix, then  $I_n = \frac{\pi^{n/2}}{|A|^{1/2}}$

If A and B are positive definite matrices, then  $|\lambda A + (1-\lambda)B| \geq |A|^\lambda |B|^{1-\lambda}$  for  $0 \leq \lambda \leq 1$ ,

perturbation of roots of polynomials, companion matrix, Hadamard's theorem, Gerishgorian Disk theorem, Taussky's theorem.

### **Recommended Books:**

- 1 Richard Bellman, Introduction to Matrix Analysis, McGraw Hill Book Company.
- 2 Franz E. Hohn, Elementary Matrix Algebra, American Publishing company Pvt. Ltd.
- 3 Shanti Narayan, A Text Book of Matrices, S. Chand and Company Ltd.
- 4 Rajendra Bhatia, Matrix Analysis, Springer.

## **THEORY OF NUMBERS-I**

Course No: **MM18106DCE**

**Examination:**

(a). Assessment

(b). Theory

Total Credits: **04**

**Total Marks: 100**

Max. Marks: 20

Max. Marks: 80

### **UNIT-I**

Divisibility, the division algorithm and its uniqueness, Greatest common divisor and its properties. The Euclidean algorithm, Prime numbers. Euclid's first theorem, Fundamental Theorem of Arithmetic, Divisor of  $n$ , Radix-representation Linear Diophantine equations. Necessary and sufficient condition for solvability of linear Diophantine equations, Positive solutions.

### **UNIT-II**

Sequence of primes, Euclid's Second theorem, Infinitude of primes of the form  $4n+3$  and of the form  $6n+5$ . No polynomial  $f(x)$  with integral coefficients can represent primes for all integral values of  $x$  or for all sufficiently large  $x$ . Fermat Numbers and their properties. Fermat Numbers are relatively prime. There are arbitrary large gaps in the sequence of primes. Congruences, Complete Residue System (CRS), Reduced Residue System (RRS) and their properties. Fermat and Euler's theorems with applications.

### **UNIT-III**

Euler's  $\phi$ -function,  $\phi(mn) = \phi(m)\phi(n)$  where  $(m, n) = 1$ ,  $\sum_{d|m} \phi(d) = n$  and

$\phi(m) = m \prod_p \left(1 - \frac{1}{p}\right)$  for  $m > 1$ . Wilson's theorem and its application to the

solution the congruence of  $x^2 \equiv -1 \pmod{p}$ , Solutions of linear Congruence's. The necessary and sufficient condition for the solution of  $a_1x_1 + a_2x_2 + \dots + a_nx_n \equiv c \pmod{m}$ . Chinese Remainder Theorem. Congruences of higher degree  $F(x) \equiv 0 \pmod{m}$ , where  $F(x)$  is a Polynomials. Congruence's with prime power, Congruences with prime modulus and related results. Lagrange's theorem, viz , the polynomial congruence  $F(x) \equiv 0 \pmod{p}$  of degree  $n$  has at most  $n$  roots.

### **UNIT-IV**

Factor theorem and its generalization. Polynomial congruences  $F(x_1, x_2, \dots, x_n) \equiv 0 \pmod{p}$  in several variables. Equivalence of polynomials. Theorem on the number of solutions of congruences: Chevalley's theorem, Warning's

theorem. Quadratic forms over a field of characteristic  $\neq 2$  Equivalence of Quadratic forms. Witt's theorem. Representation of Field Elements. Hermite's theorem on the minima of a positive definite quadratic form and its application to the sum of two, three and four squares.

**Recommended Books:**

1. W. J . Leveque, Topics in Number Theory, Vol. I and II Addition Wesley Publishing Company, INC.
2. I. Niven and H.S Zuckerman, An introduction of the Theory of Numbers.
3. Boevich and Shaferivich, Number Theory, I.R, Academic Press.

**References:**

1. T.M Apostol, Analytic Number Theory, Springer Verlag.
2. G.H Hardy and Wright, An introduction to the theory of Numbers.
3. J.P. Serre, A course in Arithmetic, GTM Vol. Springer Verlag 1973.
4. E. Landau, An Elementary Number Theory.



## **THEORY OF NUMBERS -II**

Course No: <b>MM 17204DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Integers belonging to a given exponent (mod  $p$ ) and related results, converse of Fermat's theorem; If  $d/p-1$ , the congruence  $x^d \equiv 1 \pmod{p}$ , has exactly  $d$ -solutions; If any integer belongs to  $t \pmod{p}$ , then exactly  $(t)$  incongruent numbers belong to  $t \pmod{p}$ , primitive roots, there are  $(p-1)$  primitive roots of an odd prime  $p$ , any power of an odd prime has a primitive root, the function  $\phi(m)$  and its properties,  $a^{\phi(m)} \equiv 1 \pmod{m}$ , where  $(a, m)=1$ , there is always an integer which belongs to  $(m) \pmod{m}$ , primitive  $\lambda$ -roots of  $m$ , the numbers having primitive roots are  $1, 2, 4, p$  and  $2p$ , where  $p$  is an odd prime.

### **UNIT -II**

Quadratic residues, Euler criterion, the Legendre symbol and its properties, Lemma of Gauss, the law of a quadratic reciprocity, characterization of primes of which  $2, -2, 3, -3, 5, 6$  and  $10$  are quadratic residues or non residues, Jacobi symbol and its properties, the reciprocity law for Jacobi symbol.

### **UNIT -III**

Number theoretic functions, some simple properties of  $\phi(n)$ ,  $\sigma(n)$ ,  $\tau(n)$  and  $\mu(n)$ . Mobius inversion formula. Perfect numbers. Necessary and sufficient condition for an even number to be perfect, the function  $[x]$  and its properties, average order of magnitudes of  $\phi(n)$ ,  $\sigma(n)$ ,  $\tau(n)$ , Farey fractions, rational approximation.

### **UNIT -IV**

Simple continued fractions, application of the theory of infinite continued fractions to the approximation of irrationals by rationals, Hurwitz theorem, Relation between Riemann Zeta function and the set of primes, characters, the L-Function  $L(S, \chi)$  and its properties, Dirichlet's theorem on infinity of primes in an arithmetic progression.

### **Recommended Books**

1. W. J. Leveque Topics in Number Theory, Vol. I and II Addition Wesley Publishing Company, INC.
2. I. Niven and H.S Zucherman, An introduction of the Theory of Numbers
3. Boevich and Shafeviech, Number Theory,I.R Academic Press.

### **REFERENCES:**

1. T.M Apostal, Analytic Number Theory, Springer International.
2. G.H Hardy and Wright, An introduction to the theory of Numbers.
3. J.P. Serre, A course in Arithmetic, GTM Vol. Springer Verlag 1973.
4. E. Landau, An Elementary Number Theory.

## **FOURIER ANALYSIS**

Course No: <b>MM 17205DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

#### **Fourier Series**

Motivation and definition of Fourier series, Fourier series over the interval of length  $2\pi$ , change of the interval, the complex exponential Fourier series, criteria for the convergence of Fourier series, Riemann-Lebesgue lemma, convergence at a point of continuity and at a point of discontinuity, uniform convergence and convergence in mean of the Fourier series.

### **UNIT -II**

#### **Derivatives and Integrals of Fourier Series**

Differentiation of Fourier series, differentiation of the sine and cosine series, convergence theorems related to the derived Fourier series, integration of Fourier series, applications of Fourier series to Heat flow and Vibrating string problems.

### **UNIT -III**

#### **The Fourier Transforms**

Definition and examples of Fourier transforms in  $L^1(\mathbb{R})$ , basic properties of Fourier transforms, Fourier transforms in  $L^2(\mathbb{R})$ , Convolution theorem, Plancherel's and Parseval's formulae, Poisson summation formula, Shannon-Whittaker sampling theorem, Discrete and fast Fourier transforms with examples.

## **UNIT -IV**

### **Applications of Fourier Transforms**

Application of Fourier transforms to the central limit theorem in mathematical statistics, solution of ordinary differential equations and integral equations using Fourier transforms, applications of Fourier transforms to Dirichlet's problem in the half-plane, Neumann's problem in the half-plane and Cauchy's problem for the diffusion equation.

### **Books Recommended:**

1. E.M. Stein and R. Shakarchi, Fourier Analysis, An introduction, Princeton University Press, 2002.
2. K. B. Howell, Principles of Fourier Analysis, Chapman & Hall/ CRC, Press, 2001.
3. Lokenath Debnath, Wavelet Transforms and their Applications, Birkhauser, 2002.
4. G. P. Tolstov, Fourier Series, Dover, 1972.
5. Zygmund, Trigonometric Series (2nd Ed., Volume I & II Combined), Cambridge University Press, 1959.

### **References:**

1. G. Loukas, Modern Fourier Analysis, Springer, 2011.
2. K. Ahmad and F. A. Shah, Introduction to Wavelets with Applications, Real World Education Publishers, New Delhi, 2013.
3. G. B. Folland, Fourier Analysis and Its Applications, Brooks/Cole Publishing, 1992.
4. M. Pinsky, Introduction to Fourier Analysis and Wavelets, Brooks/Cole Publishing, 2002.

## **OPERATION RESERACH**

Course No: <b>MM 17206DCE</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT –I**

Definition of operation research, main phases of OR study, linear programming problems (LPP), applications to industrial problems –optimal product links and activity levels, convex sets and convex functions, simplex method and extreme point theorems, Big M and Two phase methods of solving LPP.

### **UNIT -II**

Revised simplex method, assignment problem, Hungarian method, transportation problem, and mathematical formulation of transportation problem, methods of solving (North-West Corner rule, Vogel's method and U.V. method), concept and applications of duality, formulation of dual problem, duality theorems (weak duality and strong duality theorems), dual simplex method, primal- dual relations, complementary slackness theorems and conditions.

### **UNIT -III**

Sensitivity Analysis: changes in the coefficients of the objective function and right hand side constants of constraints, adding a new constraint and a new variable, Project management: PERT and CIM, probability of completing a project.

### **UNIT -IV**

Game theory: Two person zero sum games, games with pure strategies, games with mixed strategies, Min. Max. principle, dominance rule, finding solution of  $2 \times 2$ ,  $2 \times m$ ,  $2 \times n$  games, equivalence between game theory and linear programming problem(LPP), simplex method for game problem.

### **Recommended Books:**

- 1.C.W.Curchman, R.L. Ackoff and E.L.Arnoff, (1957) Introduction to Operation Research.
2. F. S Hiller and G.J. Lieberman, Introduction to Operations Research (Sixth Edition), McGraw Hill International, Industries Series, 1995.
3. G. Hadley, Linear programming problem, Narosa publishing House, 1995.
4. S.I.Gauss , Linear Programming, Wiley Eastern.
5. Kanti Swarup, P.K Gupta and M.M.Singh M. M, Operation Research; Sultan Chand & Sons.

## **NUMERICAL ANALYSIS**

Course No. **MM 17207DCE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Examples from ODE where analytical solution are difficult or impossible, examples from PDE where analytical solution are difficult or impossible, numerical solution of ordinary differential equations, initial value problems- Picard's and Taylor series methods – Euler's Method- Higher order Taylor methods, Modified Euler's method- Runge-Kutta methods of second and fourth order.

### **UNIT -II**

Boundary- value problems –finite difference method, forward, backward and central difference methods, second order finite difference and cubic spline methods. numerical solution of Partial differential equations, difference methods for elliptic partial differential equations – difference schemes for Laplace and Poisson's equations, difference methods for parabolic equations in one-dimensional system.

### **Recommended Books:**

1. M.K. Jain, Numerical solution of differential equations, Wiley Eastern (1979), Second Edition.
2. C.F. Gerald and P.O. Wheatley, Applied Numerical Methods, Low- priced edition, Pearson Education Asia (2002), Sixth Edition.
3. D.V. Griffiths and I.M. Smith, Numerical Methods for Engineers, Blackwell Scientific Publications (1991).

## **BIO-MATHEMATICAL MODELLING**

Course No. **MM 17208DCE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Introduction to mathematical modeling, types of modeling, classification of mathematical models, formulation, solution and interpretation of a model, linear growth and decay models, non-linear growth and decay models, continuous population models for single species, logistic growth model, discrete models, age structured populations, delay models, Fibonacci's rabbits, the golden ratio, compartment models, limitations of mathematical models.

### **UNIT -II**

Mathematical models in ecology and epidemiology: models for interacting populations, types of interactions, Lotka-Volterra system and stability analysis of the interactions like prey-predator, competition and symbiosis, infectious disease modelling, simple and general epidemic models viz SI, SIS, SIR epidemic disease models, vaccination, the SIR endemic disease model.

### **Books Recommended**

1. J. N. Kapur, Mathematical Modelling, New Age International Publishers.
2. J.D. Murray Mathematical Biology (An Introduction, Vol. I and II), Springer Verlag.
3. J.N. Kapur, Mathematical Model in Biology and Medicines.
4. S. I. Rubinow, Introduction to Mathematical Biology, John Wiley and Sons, 1975.
5. M. R. Cullen, Linear Models in Biology, Ellis Harwood Ltd.
6. Jaffrey R. Chasnov, Mathematical Biology, Hong Kong Press.

## **INTEGRAL EQUATIONS**

Course No. **MM 17209DCE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Linear integral equations of the first and second kinds, Volterra and Fredholm integral equations, relations between differential and integral equations, solution of Volterra and Fredholm integral equations by the methods of successive substitutions and successive approximations, iterated and resolvent kernels, Neumann series, reciprocal functions, Volterra's solutions of Fredholm equations.

### **UNIT -II**

Fredholm theorems, Fredholm associated equation, solution of integral equations using Fredholm's determinant and minor, homogeneous integral equations, integral equations with separable kernels, the Fredholm alternatives, symmetric kernels, Hilbert Schmidt theory for symmetric kernels, applications of integral equations to differential equations, initial value problem, boundary value problem, Dirac-Delta function, Green's function approach.

### **Books Recomendaded:**

1. R.P. Kanwal, Linear Integral Equations (Theory and Technique), Academic Press Birkhauser-1997.
2. W.V. Lovitt, Linear Integral Equations, Dover Publications, Inc. New York, 1950.
3. K.F. Riley, M.P. Hobson and S.T. Bence, Mathematical Methods for Physics and Engineering Cambridge University Press, U.K., 1997.

### **References:**

1. M.D. Raisinghania, Integral Equations and Boundary Value Problems, S.C. Chand India, 2007.
2. Shanti Swarup, Integral Equations (&Boundary Value Problems), Krishna Prakashan Media (P) Ltd. Meerut, India, 2014.



## **COMPLEX VARIABLES**

Course No. **MM 17004GE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Review of complex numbers, De-Moivre's theorem and its applications, functions of a complex variable, continuity and differentiability of complex functions, analytic functions, CR equations, complex integration, Cauchy's theorem (statement only), Cauchy's integral formulae, Liouville's theorem, Fundamental theorem of algebra.

### **UNIT -II**

Maximum modulus principle (statement only), determination of maximum modulus of  $e^z$ ,  $\sin z$ ,  $\cos z$  etc, expansion of an analytic function in a power series, Taylor's and Laurent's theorems (statements only), classification of singularities, zeros of analytic functions, argument principle, Rouché's theorem and its applications.

#### **Books Recommended:**

1. W.Rudin, Complex Analysis.
2. Ahlfors, Complex Analysis.
3. S. Ponaswamy, Foundations of Complex Analysis.
4. Schaum series, Complex Variables.

## **LATTICES AND BOOLEAN ALGEBRA**

Course No: **MM 17004OE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Lattices: Set operations, product sets, equivalence relations, relation and ordering, partially ordered sets, chain or completely ordered sets, lattices properties, lattices and algebraic systems, sub-lattices, direct product and homomorphism, modular lattices, complete lattices, distributive lattices, complemented lattices.

### **UNIT -I**

Boolean Algebra: Introduction, binary operations, algebraic structure, Boolean algebra, general properties of Boolean algebra, Boolean expressions, principle of Duality, Boolean algebra as a lattice, sub-Boolean algebra, direct product and homomorphism, representation theorem.

### **Recommended Books:**

1. Discrete Mathematics, Schaum's Outlines, Ind. Edition Tata McGraw-Hill Publishing Company Ltd. New Delhi.
2. A Text Book of Discrete Mathematics, Harish Mittal, Vinay K.Goyal, Deepak K. Goyal, I. K. Int. Publishing House Pvt. Ltd (2010).
3. Discrete Mathematical Structures, Kolman, Busby, Pross, Sixth Edition, PHI Laming Pvt. Ltd. (2010).
4. Discrete Mathematics, Richard Johnsonbaugh, sixth edition, Pearson Prentice Hall (2007).

## **LAPLACE TRANSFORMATIONS**

Course No: <b>MM 17005GE</b>	Total Credits:	<b>02</b>
	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	25

### **UNIT -I**

Laplace transform-definition, Laplace transform of some elementary functions, piecewise continuity, functions of exponential order, sufficient conditions for existence of Laplace transform, linearity property, first and second translation (shifting property), Laplace transform of derivatives, Laplace transform of integrals, periodic functions, initial and final value theorems and their generalizations, methods of finding Laplace transform, differential equations, evaluation of integrals, the Gamma function, Bessel functions, the error function, sine and cosine integrals, exponential integral, unit step function, Dirac delta function, null functions, Laplace transform of special functions.

### **UNIT -II**

Definition and uniqueness of inverse Laplace transform, Lerch's theorem, some inverse Laplace transform, some properties of Laplace transform, inverse Laplace transform of derivatives and integrals, the convolution property, methods of finding inverse Laplace transform, the complex inversion formula, the Heaviside expansion formula, the beta function, evaluation of integrals, ordinary differential equations with constant coefficients and with variable coefficients, simultaneous ordinary differential equations,

### **Recommended Books:**

1. Murrey R. Spiegel, Laplace Transforms, Schaum's outline series.

## **FOURIER TRANSFORMATIONS**

Course No: **MM 17006GE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT I**

Introduction, periodic functions, Fourier series, Dirichlet's conditions, determination of Fourier coefficients, even and odd functions and their Fourier expansion, change of interval, half range series, simple applications of the transform to one dimensional problems, Harmonic analysis.

### **UNIT II**

Fourier transform, inverse Fourier transform, Fourier sine and cosine transforms and their inversion, properties of Fourier transforms, Fourier transform of the derivative, convolution theorem, discrete Fourier transform and fast Fourier transform and their properties, applications of Fourier transform in partial differential equations with special reference to heat and wave equation.

### **Recommended Books:**

1. I. N. Sneddon: The use of Integral Transforms, McGraw-Hill, Singapore 1972.
2. R. R. Goldberg, Fourier Transforms, Cambridge University Press, 1961.
3. D. Brain, Integral Transforms and their applications, Springer, 2002
4. L. Debnath and F. A. Shah, Wavelet Transforms and their applications, Springer, 2015.

## **BASIC GRAPH THEORY**

Course No: **MM 17008GE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Introduction of graphs, paths and cycles, operations on graphs, bipartite graphs and Konigs theorem, Euler graphs and Euler's theorem, Konigsberg bridge problem, Hamiltonian graphs and Dirac's theorem, EDT, degree sequences and their characterizations, degree sets.

### **UNIT -II**

Trees and their properties, centres in trees, binary and spanning trees, degrees in trees, Cayley's theorem, fundamental cycles, generation of trees, Helly property, signed graphs, balanced signed graphs, Vertex connectivity, edge connectivity, Whitney's theorem, Planar graphs, Kuratowski's two graphs, Euler's formula, Incidence matrix  $A(G)$ , cycle matrix  $B(G)$ , fundamental cycle matrix  $B_f$ , cut-set matrix  $C(G)$ , adjacency matrix, matrix tree theorem, types of digraphs.

### **Books Recommended:**

1. R. Balakrishnan, K. Ranganathan, A Text Book of Graph Theory, Springer-Verlag, New York
2. B. Bollobas, Extremal Graph Theory, Academic Press,
3. F. Harary, Graph Theory, Addison-Wesley
4. Narsingh Deo, Graph Theory with Applications to Engineering and Computer Science, Prentice Hall
5. S. Pirzada, An Introduction to Graph Theory, Universities Press, OrientBlackswan, 2012
6. W. T. Tutte, Graph Theory, Cambridge University Press
7. D. B. West, Introduction to Graph Theory, Prentice Hall

## **NUMERICAL METHODS**

Course No: **MM18001GE**

**Examination:**

(a). Assessment

(b). Theory

Total Credits: **02**

**Total Marks: 50**

Max. Marks: 10

Max. Marks: 40

### **UNIT -I**

Solution of algebraic and transcendental and polynomial equations, bisection method, iteration method based on first degree equation, secant method, regula-falsi method, Newton-Raphson method, rate of convergence of Newton-Raphson method & secant method, system of linear algebraic equation, Gauss elimination method, Gauss Jordan method.

### **UNIT -II**

Interpolation and approximation of finite difference operators, Newton's forward, backward interpolation, central difference interpolation, Lagrange's interpolation, Newton Divided Difference interpolation, Hermite interpolation, Spline interpolation, numerical differentiation and Integration.

### **Recommended Books:**

1. M.K. Jain, Numerical solution of differential equations, Wiley Eastern (1979), Second Edition.
2. D.V. Griffiths and I.M. Smith, Numerical Methods for Engineers, Blackwell Scientific Publications (1991).

### **REFERENCES:**

1. S.C. Chapra, and P.C. Raymond, Numerical Methods for Engineers, Tata McGraw Hill, New Delhi (2000)
2. R.L. Burden, and J. Douglas Faires, Numerical Analysis, P.W.S. Kent Publishing Company, Boston (1989), Fourth edition.
3. S.S. Sastry, Introductory methods of Numerical analysis, Prentice-Hall of India, New Delhi (1998).
4. M.K. Jain, S.R.K. Iyengar and R.K. Jain, Numerical methods for scientific and Engineering computation, Wiley Eastern (1993)

## **CALCULUS**

Course No: **MM18001OE**

**Examination:**

(a). Assessment

(b). Theory

Total Credits: **02**

**Total Marks: 50**

Max. Marks: 10

Max. Marks: 40

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### **UNIT -I**

Functions, the idea of limits, techniques for computing limits, infinite limits, continuity, derivative, rules for differentiation, derivatives as rate of change, applications of the derivative, maxima and minima, increasing and decreasing functions, mean value theorem and its applications, indeterminate forms, partial differentiation, Euler's theorem.

### **UNIT -II**

Indefinite integral, techniques of integration, definite integral, area of a bounded region, first Order ordinary differential equations and their solutions, variables separable method, homogeneous form, equations reducible to homogeneous form, linear differential equations of the form  $dy/dx + Py = Q$  and equations reducible to this form.

**Recommended Books:**

1. A.Aziz, S.D.Chopra and M.L.Kochar, Differential Calculus, Kapoor Publications.
2. William L.Briggs and Lyle Cochran, Calculus, Pearson.
3. S.D.Chopra and M.L.Kochar, Integral Calculus, Kapoor Publications.
4. R.K.Jain and S.R.K. Lyengar, Advanced Engineering Mathematics, Narosa.

## **INTRODUCTION TO MATHEMATICAL MODELLING**

Course No: **MM 17003OE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Introduction to mathematical modeling, types of modeling, classification of mathematical models, formulation, solution and interpretation of a model, models in population dynamics, linear growth and decay models, non-linear growth and decay models, continuous population models for single species, delay models, logistic growth model, discrete models, age structured populations, Fibonacci's rabbits, the golden ratio, compartment models, limitations of mathematical models.

### **UNIT -II**

Mathematical modeling through system of ordinary differential equations, compartment models through system of ODE's, modeling in economics, medicine, international trade, gravitation; planetary motion; basic theory of linear difference equations with constant coefficients, mathematical models through difference equations in population dynamics, finance and genetics, modeling through graphs.

#### **Books Recommended:**

1. J. N. Kapur, Mathematical Modelling, New Age International Publishers.
2. Neil Gerschenfeld : The nature of Mathematical modeling, Cambridge University Press, 1999.
3. A. C. Fowler : Mathematical Models in Applied Sciences, Cambridge University Press, 1997.
4. M. R. Cullen, Linear Models in Biology, Ellis Harwood Ltd.
5. J.N. Kapur, Mathematical Model in Biology and Medicines.



## **INTRODUCTION TO NUMBERS**

Course No. **MM 17001OE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Number system, basic binary operations, ordering of integers, well ordering principle, principle of mathematical induction, radix representations, divisibility, greatest common divisor (gcd), least common multiple (lcm) and their properties, pigeonhole principle.

### **UNIT -I**

Prime and composite numbers, relatively prime numbers, infinitude of prime numbers, primes of different forms, perfect numbers, fundamental theorem of arithmetic, congruence's and their properties.

### **Recommended Books:**

1. W.J.Leveque, Topics in Number Theory, Addison Wesley Publishing Company.
2. Ivan Niven & H.S.Zuckerman, An introduction to the Theory of Numbers, Wiley Eastern Ltd.
3. G.H.Hardy & E.M.Wright, An introduction to the Theory of Numbers, Oxford University Press 1954.
4. H.N.Wright, First Course in Theory of Numbers, John Wiley & Sons, New York 1939.

## **APPLIED GROUP THEORY**

Course No: **MM 17007GE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT - I**

Basic concepts of relations and functions, binary operation, types and properties of functions, groups, sub-groups, normal subgroups, Cyclic groups and their properties; Homomorphism and Isomorphism, permutation groups, cosets and Lagrange and Cayley's theorems (statements only), Quotient groups and the homomorphism theorem, action of groups on sets, applications of groups through geometric patterns.

### **UNIT- II**

Alternating groups and their properties, symmetry groups in Euclidean space, motivation, isometries of n-space, the finite subgroups, representation theory, linear representations of groups, decomposing displacements, some compact lie groups and their representations, some examples of Lie groups, representation theory of compact Lie groups.

### **Recommended Books:**

1. G. Birkhoff and T. C. Bartee, Modern Applied Algebra, Mc-Graw Hill.
2. Arjeh Cohen, Rosane Ushirobira and Jan Draisma, Group theory for Maths, Physics and Chemistry Students.
3. J. A. Gallian, Contemporary Modern Algebra.
4. Surjeet Singh and Qazi Zameer-ud-Din, Modern Algebra.
5. P. M. Cohn, Lie Groups.

## **MATRIX ALGEBRA**

Course No. **MM 17002OE**  
End Term Exam: (2 Credits)

Total Credits: **02**  
Max.Marks: **50**

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### **UNIT -I**

Matrices, types, adjoint and inverse of a matrix, partition of a matrix, matrix polynomials, characteristic equation of a matrix, Caley Hamilton theorem, elementary transformations, rank of a matrix, determination of rank.

### **UNIT - II**

Normal form with examples, solution of equations, homogenous and non-homogeneous equations, linear dependence and independence, orthogonal and unitary matrices and their determination, eigen values and eigen vectors and their determination, similarity of matrices with examples.

### **Books Recommended**

- 5 Franz E. Hohn, Elementary Matrix Algebra, American Publishing company Pvt.ltd.
- 6 Shanti Narayan, A Text Book of Matrices, S. Chand and company Ltd.
- 7 Rajendra Bhatia , Matrix Analysis Springer.
- 8 A.Aziz, N.A.Rather and B.A.Zargar, Elementary Matrix Algebra , KBD.

## **SEMESTER-I**

### **ADVANCED ABSTRACT ALGEBRA-I**

Course No: **MM18101CR**

Examination:

(a). Assessment

(b). Theory

Total Credits: **04**

Total Marks: 100

Max. Marks: 20

Max. Marks: 80

#### **UNIT-I**

Definitions and examples of semi-groups and monoids, criteria for the semi-groups to be a group, cyclic groups, structure theorem for cyclic groups, endomorphism, automorphism, inner automorphism and outer automorphism, center of a group, Cauchy's and Sylow's theorem for abelian groups, permutation groups, symmetric groups, alternating groups, simple groups, simplicity of the alternating group  $A_n$  for  $n \geq 5$ .

#### **UNIT-II**

Normalizer, conjugate classes, class equation of a finite group and its applications, Cauchy's and Sylow's theorems for finite groups, double cosets, second and third parts of Sylow's theorem, direct product of groups, finite abelian groups, normal and subnormal series, composition series, Jordan Holder theorem for finite groups, Zassenhaus lemma, Schreier's refinement theorem, Solvable groups.

#### **UNIT-III**

Brief review of rings, integral domain, ideals, the field of quotients of an integral domain, embedding of an Integral domain, Euclidean rings with examples such as  $\mathbb{Z}[\sqrt{-1}]$ ,  $\mathbb{Z}[\sqrt{2}]$ , principal ideal rings(PIR), unique factorization domains(UFD) and Euclidean domains, greatest common divisor, lowest common multiple in rings, relationships between Euclidean rings, P.I.R.'s and U.F.D.

#### **UNIT-IV**

Polynomial rings, the division algorithm for polynomials, irreducible polynomials, polynomials and the rational field, primitive polynomials, contraction of polynomials, Gauss lemma, Integer monic polynomial, Eisenstein's irreducibility criterion, cyclotomic polynomials, polynomial rings and commutative rings.

#### **Recommended Books**

1. P. B. Bhattacharaya and S.K.Jain, Basic Abstract Algebra.
2. J. B. Fraleigh, A First Course in Abstract Algebra.
3. J. A. Gallian, Contemporary Abstract Algebra.
4. I. N. Herstein, Topics in Algebra.

5. K. S. Miller, Elements of Modern Abstract Algebra.
6. Surjeet Singh and Qazi Zameer-ud-Din, Modern Algebra, Vikas Publishing House Private Limited.

## **REAL ANALYSIS - I**

Course No: **MM18102CR**

Examination:

(a). Assessment

(b). Theory

Total Credits: **04**

Total Marks: 100

Max. Marks: 20

Max. Marks: 80

### **UNIT-I**

Integration : Definition and existence of Riemann – Stieltje’s integral , behavior of upper and lower sums under refinement, necessary and sufficient conditions for RS-integrability of continuous and monotonic functions, reduction of an RS-integral to a Riemann integral, basic properties of RS-integrals, differentiability of an indefinite integral of continuous functions, the fundamental theorem of calculus for Riemann integrals.

### **UNIT-II**

Improper integrals: integration of unbounded functions with finite limit of integration, comparison tests for convergence, Cauchy’s test, infinite range of integration, absolute convergence, integrand as a product of functions, Abel’s and Dirichlet’s test.

Inequalities: arithmetic-geometric means equality, inequalities of Cauchy Schwartz, Jensen, Holder & Minkowski, inequality on the product of arithmetic means of two sets of positive numbers.

### **UNIT-III**

Infinite series: Carleman’s theorem, conditional and absolute convergence, multiplication of series, Merten’s theorem, Dirichlet’s theorem, Riemann’s rearrangement theorem. Young’s form of Taylor’s theorem, generalized second derivative, Bernstein’s theorem and Abel’s limit theorem.

### **UNIT-IV**

Sequences and series of functions: point wise and uniform convergence, Cauchy criterion for uniform convergence,  $M_n$ -test, Weiestrass M-test, Abel’s and Dirichlet’s test for uniform convergence, uniform convergence and continuity, R- integration and differentiation, Weiestrass approximation theorem, example of continuous nowhere differentiable functions.

### **Recommended Books:**

1. R. Goldberg, Methods of Real Analysis.
2. W. Rudin, Principles of Mathematical Analysis.
3. J. M. Apostol, Mathematical Analysis.
4. S.M.Shah and Saxen, Real Analysis.
5. A.J.White, Real Analysis , An Introduction.
6. L.Royden, Real Analysis.
7. S.C.Malik and Gupta, Real Analysis

## **TOPOLOGY**

Course No: **MM18103CR**

**Examination:**

(a). Assessment

(b). Theory

Total Credits: **04**

**Total Marks: 100**

Max. Marks: 20

Max. Marks: 80

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### **UNIT-I**

Review of countable and uncountable sets, Schroeder-Bernstein theorem, axiom of choice and its various equivalent forms, definition and examples of metric spaces, open and closed sets, completeness in metric spaces, Baire's category theorem, and applications to the (i) non-existence of a function which is continuous precisely at irrationals (ii) impossibility of approximating the characteristic of rationals on  $[0, 1]$  by a sequence of continuous functions.

### **UNIT -II**

Completion of a metric space, Cantor's intersection theorem with examples to demonstrate that each of the conditions in the theorem is essential, uniformly continuous mappings with examples and counter examples, extending uniformity continuous maps, Banach's contraction principle with applications to the inverse function theorem in  $\mathbb{R}$ .

### **UNIT T-III**

Topological spaces; definition and examples, elementary properties, Kuratowski's axioms, continuous mappings and their characterizations, pasting lemma, convergence of nets and continuity in terms of nets, bases and sub bases for a topology, lower limit topology, concepts of first countability, second countability, separability and their relationships, counter examples and behavior under subspaces, product topology and weak topology, compactness and its various characterizations.

### **UNIT -IV**

Heine-Borel theorem, Tychonoff's theorem, compactness, sequential compactness and total boundedness in metric spaces, Lebesgue's covering lemma, continuous maps on a compact space, separation axioms  $T_i$   $\left(i = 1, 2, 3, 3\frac{1}{2}, 4\right)$  and their permanence properties, connectedness, local connectedness, their relationship and basic properties, connected sets in  $\mathbb{R}$ ,

Urysohn's lemma, Urysohn's metrization theorem, Tietze's extension theorem, one point compactification.

**Recommended Books:**

1. G.F.Simmons, Introduction to Topology and Modern Analysis.
2. J. Munkres, Topology.
3. K.D. Joshi, Introduction to General Topology.
4. J.L.Kelley, General Topology.
5. Murdeshwar, General Topology.
6. S.T. Hu, Introduction to General Topology.



## **THEORY OF PROBABILITY**

Course No: **MM18104CR**

Total Credits: **02**

**Examination:**

**Total Marks: 50**

(a). Assessment

Max. Marks: 10

(b). Theory

Max. Marks: 40

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### **UNIT-I**

The probability set functions, its properties, probability density function, the distribution function and its properties, mathematical expectations, some special mathematical expectations, inequalities of Markov, Chebyshev and Jensen.

### **UNIT-II**

Conditional probability, independent events, Baye's theorem, distribution of two and more random variables, marginal and conditional distributions, conditional means and variances, correlation coefficient, stochastic independence and its various criteria.

### **Recommended Books:**

1. Hogg and Craig, An Introduction to the Mathematical Statistics.
2. Mood and Grayball, An Introduction to the Mathematical Statistics.

## **FUNCTIONAL ANALYSIS-I**

Course No: <b>MM 17303CR</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **BANACH SPACE:**

#### **UNIT -I**

Banach Spaces: definition and examples, subspaces, quotient spaces, continuous linear operators and their characterization, completeness of the space  $L(X, Y)$  of bounded linear operators (and its converse), incompleteness of  $C[a, b]$ , under the integral norm, finite dimensional Banach spaces, equivalence of norms on finite dimensional space and its consequences, dual of a normed linear space, Hahn Banach theorem (extension form) and its applications, complemented subspaces, duals of  $l_p^n$ ,  $C_0$ ,  $l_p$  ( $p \geq 1$ ),  $C[a, b]$ .

#### **UNIT -II**

Uniform boundedness, principle and weak boundedness, dimension of an  $\infty$ -dimensional Banach space, conjugate of a continuous linear operator and its properties, Banach-Steinhaus theorem, open mapping and closed graph theorems, counterexamples to Banach-Steinhaus, open mapping theorem and closed graph theorems for incomplete domain and range spaces, separable Banach spaces and the separability of some concrete Banach spaces ( $C_0$ ,  $C[0, 1]$ ,  $l_p$ ,  $p \geq 1$ ), reflexive Banach Spaces, closed subspace and the dual of a reflexive Banach space, examples of reflexive and non-reflexive Banach spaces.

#### **UNIT -III**

### **HILBERT SPACE:**

Hilbert spaces: definition and examples, Cauchy's Schwartz inequality, parallelogram law, orthonormal (o.n) systems, Bessel's inequality and Parseval's Identity for complete orthonormal systems, Riesz-Fischer theorem, Gram Schmidt process, o.n basis in separable Hilbert spaces.

## **UNIT -IV**

Projection theorem, Riesz Representation theorem, counter example to the projection theorem and Riesz representation theorem for incomplete spaces, Hilbert property of the dual of a Hilbert space and counter examples of incomplete inner product spaces, reflexivity of Hilbert space, adjoint of a Hilbert space operator, weak convergence and Bolzano-Weirstrass property in Hilbert Spaces, normal and unitary operators, finite dimensional spectral theorem for normal operators.

### **Recommended Books:**

1. B.V.Limaya, Functional Analysis.
2. C.Goffman G. Pedrick, A First Course in Functional Analysis.
3. L.A. Lusternick & V.J. Sobolov, Elements of Functional Analysis.
4. J.B. Conway, A Course in Functional Analysis.

## **DIFFERENTIAL GEOMETRY**

Course No: <b>MM 17402CR</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Curves: differentiable curves, regular point, parameterization of curves, arc-length, arc-length is independent of parameterization, unit speed curves, plane curves, curvature of plane curves, osculating circle, centre of curvature. computation of curvature of plane curves, directed curvature, examples, straight line, circle, ellipse, tractrix, evolutes and involutes, space curves, tangent vector, unit normal vector and unit binormal vector to a space curve, curvature and torsion of a space curve, the Frenet-Serret theorem, first fundamental theorem of space curves, intrinsic equation of a curve, computation of curvature and torsion, characterization of helices and curves on sphere in terms of their curvature and torsion, evolutes and involutes of space curves.

### **UNIT -II**

Surfaces: regular surfaces with examples, coordinate charts or curvilinear coordinates, change of coordinates, tangent plane at a regular point, normal to the surface, orientable surface, differentiable mapping between regular surfaces and their differential, fundamental form or a metric of a surface, line element, invariance of a line element under change of coordinates, angle between two curves, condition of orthogonality of coordinate curves, area of bounded region, invariance of area under change of coordinates.

### **UNIT -III**

Curvature of a Surface: normal curvature, Euler's work on principal curvature, qualitative behavior of a surface near a point with prescribed principal curvatures, the Gauss map and its differential, the differential of Gauss is self-adjoint, second fundamental form, normal curvature in terms of second fundamental form. Meunier theorem, Gaussian curvature, Weingarten equation, Gaussian curvature  $K(p) = (eg-f^2)/EG-F^2$ , surface of revolution, surfaces with constant positive or negative Gaussian curvature, Gaussian curvature in terms of area, line of curvature, Rodrigue's formula for line of curvature, equivalence of surfaces, isometry between surfaces, local isometry, and characterization of local isometry.

## UNIT -IV

Christoffel symbols, expressing Christoffel symbols in terms of metric coefficients and their derivative, Theorema egregium (Gaussian curvature is intrinsic), isometric surfaces have same Gaussian curvatures at corresponding points, Gauss equations and Manardi Codazzi equations for surfaces, fundamental theorem for regular surface. (Statement only).

Geodesics: geodesic curvature, geodesic curvature is intrinsic, equations of geodesic, geodesic on sphere and pseudo sphere, geodesic as distance minimizing curves. Gauss-Bonnet theorem (statement only), geodesic triangle on sphere, implication of Gauss-Bonnet theorem for geodesic triangle.

### **Recommended Books:**

1. John Mc Cleary, Geometry from a differentiable Viewpoint. (Cambridge Univ. Press).
2. W. Klingenberg, A course in Differential Geometry (Spring Verlag).
3. C. E. Weatherburn, Differential Geometry of Three dimensions.
4. T. Willmore, An Introduction to Differential Geometry.
5. J. M. Lee, Riemannian Manifolds, An Introduction to Curvature.

## **REAL ANALYSIS - II**

Course No: <b>MM 17202CR</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

### **UNIT -I**

Measure theory: definition of outer measure and its basic properties, outer measure of an interval as its length, countable additivity of the outer measure, Borel measurable sets and Lebesgue measurability of Borel sets, Cantor set, existence of non-measurable sets and of measurable sets which are not Borel, outer measure of monotonic sequences of sets.

### **UNIT -II**

Measurable functions and their characterization, algebra of measurable functions, Stienhauss theorem on sets of positive measure, Ostrovisk's theorem on measurable solution of  $f(x+y) = f(x) + f(y)$ ,  $x, y \in \mathbb{R}$ , convergence a.e., convergence in measure and almost uniform convergence, their relationship on sets of finite measure, Egoroff's theorem.

### **UNIT -III**

Lebesgue integral of a bounded function, equivalence of L-integrability and measurability for bounded functions, Riemann integral as a Lebesgue integral, basic properties of Lebesgue -integral of a bounded function, fundamental theorem of calculus for bounded derivatives, necessary and sufficient condition for Riemann integrability on  $[a, b]$ , L- integral of non-negative measurable functions and their basic properties, Fatou's lemma and monotone convergence theorem, L-integral of an arbitrary measurable function and basic properties, dominated convergence theorem and its applications.

### **UNIT -IV**

Absolute continuity and bounded variation, their relationships and counter examples, indefinite integral of an L-integrable function and its absolute continuity, necessary and sufficient condition for bounded variation, Vitali's covering lemma and a.e., differentiability of a monotone function  $f$  and  $\int f' \leq f(b) - f(a)$ .

**Recommended Books:**

1. L. Royden, Real Analysis (PHI).
2. R. Goldberg, Methods of Real Analysis.
3. G. De. Barra, Measure theory and Integration ( Narosa).
4. I. K. Rana , An Introduction to Measure and Integration.
5. W. Rudin, Principles of Mathematical Analysis.
6. Chae, Lebesgue Integration.
7. T. M. Apostol, Mathematical Analysis.
8. S. M. Shah and Saxena, Real Analysis.

## **SEMESTER-II**

### **DISCRETE MATHEMATICS**

Course No: <b>MM 17201CR</b>	Total Credits:	<b>04</b>
Continuous Exam-I (1 Credit)	Max.Marks:	25
Continuous Exam-II (1 Credit)	Max.Marks:	25
End Term Exam: (2 Credits)	Max.Marks:	50

#### **UNIT -I**

##### **Graphs, traversability and degrees**

Introduction of graphs, paths and cycles, operations on graphs, bipartite graphs and Konigs theorem, Euler graphs and Euler's theorem, Konigsberg bridge problem, Hamiltonian graphs and Dirac's theorem, degree sequences, Wang-Kleitman theorem, Havel-Hakimi theorem, Hakimi's theorem, Erdos-Gallai theorem, degree sets.

#### **UNIT -II**

##### **Trees and Signed graphs**

Trees and their properties, centres in trees, binary and spanning trees, degrees in trees, Cayley's theorem, fundamental cycles, generation of trees, Helly property, signed graphs, balanced signed graphs and characterizations.

#### **UNIT -III**

##### **Connectivity and Planarity**

Cut-sets and their properties, vertex connectivity, edge connectivity, Whitney's theorem, Menger's theorem (vertex and edge form), properties of a bond, block graphs, planar graphs, Kuratowski's two graphs, embedding on a sphere, Euler's formula, Kuratowski's theorem, geometric dual, Whitney's theorem on duality, regular polyhedras.

#### **UNIT -IV**

##### **Matrices and Digraphs**

Incidence matrix  $A(G)$ , modified incidence matrix  $A_f$ , cycle matrix  $B(G)$ , fundamental cycle matrix  $B_f$ , cut-set matrix  $C(G)$ , fundamental cut set matrix  $C_f$ , relation between  $A_f$ ,  $B_f$  and  $C_f$ , path matrix, adjacency matrix, matrix tree theorem, types of digraphs, types of connectedness, Euler digraphs,



Hamiltonian digraphs, arborescence, matrices in digraphs, Camions theorem, tournaments, characterization of score sequences, Landau's theorem, oriented graphs and Avery's theorem.

**Recommended Books:**

1. R. Balakrishnan, K. Ranganathan, A Text Book of Graph Theory, Springer-Verlag, New York.
2. B. Bollobas, Extremal Graph Theory, Academic Press.
3. F. Harary, Graph Theory, Addison-Wesley.
4. Narsingh Deo, Graph Theory with Applications to Engineering and Computer Science, Prentice Hall.
5. S. Pirzada, An Introduction to Graph Theory, Universities Press, Orient Blackswan, 2012.
6. W. T. Tutte, Graph Theory, Cambridge University Press.
7. D. B. West, Introduction to Graph Theory, Prentice Hall.